

# HIGHER: Key Stage 4 Maths Curriculum

## Long term plan Year 9

Autumn 1	
<b>Chapter 1: Calculations</b>	<b>Chapter 2: Expressions</b>
<b>Assessment:</b> Chapter Test A	<b>Assessment:</b> Chapter Test A
<b>Builds Upon:</b> <ul style="list-style-type: none"><li>• Order integers, decimals and negative numbers</li><li>• Round to nearest 10, 100, 1000</li><li>• Round to decimal places</li><li>• Add/Subtract numbers with decimals</li><li>• Multiply numbers with decimals</li><li>• Divide using the algorithm (by hand)</li><li>• Divide decimal numbers using the algorithm</li><li>• Order of Operations (BIDMAS)</li></ul>	<b>Builds Upon:</b> <ul style="list-style-type: none"><li>• Apply algebraic notation to write simple expressions</li><li>• Simplify expressions by collecting like terms (addition and subtraction)</li><li>• Apply the Index laws (multiplication, division)</li><li>• Apply the Index laws (fractional, negative and zero)</li><li>• Expanding single brackets Expand two single brackets and simplify</li><li>• Factorise single brackets</li></ul>
<b>Introduces:</b> <ul style="list-style-type: none"><li>• Rounding to significant figures</li><li>• Estimate by rounding to one significant figure</li><li>• Add/Subtract negative numbers</li><li>• Multiply/Divide negative numbers</li><li>• Manipulate of operations involving decimals (using one calculation to find the answer to another)</li></ul>	<b>Introduces:</b> <ul style="list-style-type: none"><li>• Simplifying algebraic fractions Add/Subtract algebraic fractions</li><li>• Multiplying algebraic fractions</li><li>• Divide algebraic fractions</li></ul>

## Autumn 2

### Chapter 3: Angles and Polygons

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Measure and describe angles as acute, right, obtuse or reflex
- Describe and apply the properties of angles around a point (sum of 360 degrees)
- Describe and apply the properties of angles on a straight line (sum of 180 degrees)
- Derive and apply the sum of angles in triangles and quadrilaterals
- Calculate interior angles in polygons (using angles in a triangle)
- Deduce and apply the sum of interior angles of any polygon and use  $(n-2)*180$

#### **Introduces:**

- Calculate bearings based on angles around a point
- Describe and apply the equivalence of vertically opposite angles
- Identify and apply the properties of angles in parallel lines (alternate, corresponding and co-interior rules)
- Apply knowledge of special triangles to derive angles
- Solve problems involving all of the above (providing reasons)
- Identify similarity between shapes
- Calculate and apply scale factors
- Identify and describe types of congruence (SSS, SAS, ASA, RHS)
- Apply similarity and congruence to problem solve
- Calculate and apply scale factors for area and volume from the linear scale factor
- Calculate exterior angles in polygons
- Solve problems involving angles in polygons

## Spring 1

### Chapter 4: Handling Data 1

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Construct and interpreting bar charts
- Construct and interpret two way tables
- Calculate the mean, mode and median of listed data
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#### **Introduces:**

- Construct and interpret pie charts
- Calculate the mean, mode and median of data in a frequency table
- Understand the advantages and disadvantages of different averages
- Calculate the range and interquartile range
- Identify outliers and explain their effect on averages/ranges
- Compare distributions using averages and range
- Construct frequency tables for grouped data
- Construct and interpret Histograms with equal widths
- Construct and interpret Histograms with unequal class widths
- Calculate frequency density

## Spring 2

### Chapter 5: Fractions Decimals and Percentages

### Chapter 6: Formulae & Functions

**Assessment:** Chapter Test A

**Assessment:** Chapter Test A

#### Builds Upon:

- Name and construct fraction diagrams
- Convert between improper fractions and mixed numbers
- Identify and create equivalent fractions
- Simplifying fractions
- Write fractions as decimals
- Order fractions and mixed numbers
- Calculate fractions of amounts
- Calculating percentages of amounts
- Multiplying fractions, including simplifying (cancelling common factors)
- Multiplying fractions and mixed numbers
- Dividing fractions and mixed numbers
- Adding and subtracting fractions with the same denominator
- Adding and subtracting fractions with different denominators
- Adding and subtracting mixed numbers
- Solve worded fraction problems
- Write percentages as fractions and decimals
- Converting between fractions, decimals and percentages
- Compare using  $<$  or  $>$  and order fractions, decimals and percentages

#### Builds Upon:

- Write formulae from sentences
- Substitute to solve (positive and negative numbers)
- Use standard formulae (e.g. kinematics)
- Simplify expressions
- Expand single brackets
- Simplify algebraic fractions

#### Introduces:

- Convert recurring decimals to fractions
- Solving complex worded problems with a mixture of fractions, decimals and percentages

#### Introduces:

- Change the subject of formulae
- Construction mapping diagrams for functions
- Write the inverse of a function  $f(x) \rightarrow f^{-1}(x)$
- Write and solve composite functions
- Identify expressions, equations, inequalities, formulae and identities
- Prove identities and find missing values  
Prove statements to be true or false
- Expand double brackets
- Factorise quadratic expressions
- Distinguishing between, and factorise :  $x^2 - 4$  and  $x^2 - 4x$
- Complete the difference of two squares

## Summer 1

### Chapter 7: Working in 2D

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Accurately measure and draw line segments and angles
- Bearings on a map
- Area of quadrilaterals (squares/rectangles/parallelograms/trapeziums) and triangles
- Area of compound 2D shapes

#### **Introduces:**

- Apply scale to drawings -find distances on a map and in real life
- Sketching lines such as  $y = -2$ ,  $y = x$  etc.
- Completing transformations:
  - Translations
  - Reflections
  - Rotations from origin and a point
  - Enlargements (scale factor greater than 1, between 0 and 1, & negative)
  - Enlargements from a point
  - Combinations of Transformations
- Describing transformations

## Summer 2

### Chapter 8: Probability

### Chapter 9: Estimation and Approximation

**Assessment:** Chapter Test A

**Assessment:** Chapter Test A

**Builds Upon:**

- Understand the probability scale
- Construct sample space diagrams  
List sample space of an experiment
- Write experimental and theoretical probabilities as fractions

**Builds Upon:**

- Round to appropriate degree of accuracy (10,100,1000s, dps, sfs)
- Use approximation to make estimates
- Check calculations using approximation and estimation
- Use common calculator functions
- Convert units of length, mass, volume, capacity, time and area
- Calculate the upper and lower bounds of rounded values

**Introduces:**

- Write experimental and theoretical probabilities as relative frequencies
- Calculate expected frequencies
- Compare theoretical probabilities with experimental probabilities
- Recognise mutually exclusive events and exhaustive events
- Understand that the probabilities of mutually exclusive exhaustive events sum to one
- Compare bias and equally likely events

**Introduces:**

- Estimate square roots
- Calculate compound units of speed and density
- Rearrange compound unit calculations to find missing values
- Use inequality notation to state error intervals and interpret limits of accuracy

# Year 10

## Autumn 1

### Chapter 10: Equations and Inequalities

#### Assessment: Chapter Test A

#### Builds Upon:

- Solving two step equations (brackets, negatives)
- Solving equations involving fractions (and implied brackets)
- Solving equations with the unknown on both sides
- Forming and solving equations
- Solving by completing the square
- Solving by applying the quadratic formula
- Forming and solving quadratic equations
- Solving simultaneous equations graphically
- Solving simultaneous equations using elimination
  
- Solving equations using trial and improvement
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#### Introduces:

- Solving quadratics graphically for the roots (x intercepts)
- Solving quadratics with/without coeff of  $x^2$  by factorising
- Solving simultaneous equations using substitution
- Solving simultaneous equations between a linear and quadratic
- Forming and solving simultaneous equations
- Using iteration formulae to find a solution to a given number of decimal places

## Autumn 2

### Chapter 11: Circles and Constructions

**Assessment:** Chapter Test A

**Builds Upon:**

- Circumference of circles
- Area of circles
- Circumference and area of composite shapes involving parts of circles
- Construct angle
- Construct line bisectors (of a line, from a point to a line, from a point on a line)
- Construct triangles
- Construct quadrilaterals,
- Construct an angle of 60 degrees
- Construct loci from points, lines, around shapes etc.
- Construct loci involving a change of radius or rolling shapes etc.

**Introduces:**

- Arc length
- Area of sectors
- Perimeter and area of composite shapes involving sectors
- Circle Theorems
- Proof of circle theorems

## Spring 1

### Chapter 12: Ratio and proportion

### Chapter 13: Factors, powers and roots

**Assessment:** Chapter Test A

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Express proportions of an amounts as fractions or percentages
- Calculate percentage increases and decreases using multiplication
- Find the original value follow a percentage increases and decreases
- Simplify ratios
- Write ratios from worded questions

#### **Builds Upon:**

- Know and use the language of prime numbers, factors and multiples
- Write a number as the product of its prime factors (prime decomposition)
- Construct a prime factor venn
- Identify HCF
- Identify LCM
- Find square and cube roots of numbers and apply law of indices
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#### **Introduces:**

- Share amounts into a ratio (ADAM)
- Use scale factors, scale diagrams and maps.
- Understand and calculate simple interest

#### **Introduces:**

- Estimate the square or cube root of an integer
- Simplify expressions involving surds
- Rationalise fractions involving surds

## Spring 2

### Chapter 14: Graphs 1

**Assessment:** Chapter Test A

**Builds Upon:**

- Equation of a straight line  $y=mx+c$
- Calculating gradient
- Identifying y intercept
- Graphing linear equations
- Writing the equation for linear graphs
- Properties of parallel and perpendicular lines
- Writing the equations for parallel and perpendicular lines
- Equation of quadratic curves  $ax^2+bx+c=y$
- Graph quadratic equations
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**Introduces:**

- Identifying x intercepts (roots) and y intercepts graphically and algebraically
- Identifying turning points graphically and algebraically
- Properties of quadratic functions
- Kinematic graphs (solving distance, speed and acceleration problems)
- Solving Inequalities
- Graphing Inequalities

### Chapter 15: Working in 3D

**Assessment:** Chapter Test A

**Builds Upon:**

- Draw and interpret net diagrams
- Calculate surface area of 3D shapes
- Draw and interpret plans and elevation of 3D shapes
- Calculate volume of a right prism
- Calculate volume of a cylinder

**Introduces:**

- Apply compound units to calculate mass ( $m=vd$ )
- Calculate the volume of frustums, spheres, hemispheres, pyramids and cones
- Apply reasoning and problem solving

## Summer 1

**PPES**

**Chapter 16: Handling Data 2**

**Assessment** 2x 90 minute PPEs

**Assessment:** Chapter Test A

**Builds Upon:**

- Calculate estimated mean, modal class and class interval of the median for grouped data
- Construct scatter graphs and describe correlation
- Make predictions based on the correlation (interpolation vs. extrapolation)
- Construct time series graphs
- Discuss any short term trends, seasonal variation and longer term trends
- Construct histograms
- Solve frequency density problems using histograms

**Introduces:**

- Construct and interpret box plots
- Construct and interpret cumulative frequency graphs

Compare spread using box plots

## Summer 2

### Chapter 17: Calculations 2

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Convert in and out of index form
- Solve calculations involving index laws (including roots, negatives, fractional indices)
- Convert in and out of standard form
- Solve calculations in standard form

#### **Introduces:**

- Simplify and manipulate surds
- Solve calculations involving fractions, surds and pi
- Construction mapping diagrams for functions
- Write the inverse of a function  $f(x) \rightarrow f^{-1}(x)$
- Write and solve composite functions

### Chapter 18: Graphs 2

**Assessment:** Chapter Test A

#### **Builds Upon:**

- Graphing linear and quadratics equations
- Sketching translations (including reflections, transformations etc.)

#### **Introduces:**

- Recognise and plot graphs of cubic functions
- Recognise and plot graphs of reciprocal functions
- Recognise and sketch graphs of exponential functions
- Recognise and sketch trigonometric functions
- To recognise and sketch translation and reflections of graphs
- Draw and interpret non-standard graphs of real-life situations
- Gradients and areas under graphs
- Equation of a circle
- Find the tangent to a circle at a point

# Year 11

## Autumn 1

### Chapter 19: Pythagoras, Trigonometry and Vectors

**Assessment:** Chapter A Test

#### **Builds Upon:**

- Apply Pythagoras' theorem to find long sides
- Apply Pythagoras' theorem to find short sides

#### **Introduces:**

- Apply Pythagoras' theorem to find distance between two points
- Apply trigonometric ratios (sin/cos/tan) to find missing sides in right angle triangles
- Apply trigonometric ratios (sin/cos/tan) to find missing angles in right angle triangles
- Know the exact values of  $\sin\theta$  and  $\cos\theta$  for  $\theta = 0, 30, 45, 60, 90$  degrees
- Know the exact value of  $\tan\theta$  for  $\theta = 0, 30, 45, 60$  degrees
- Apply the sine rule to find missing lengths and angles
- Apply the cosine rule to find missing lengths and sides
- Apply sine formula for the area of non right angle triangles
- Solve 3D Pythagoras' theorem and trigonometry problems
- Write column vectors and draw vector diagrams
- Add and subtract vectors
- Calculate multiples of vectors using a scalar
- Use vectors in geometric proofs

## Autumn 2

PPES	Chapter 20 Combined Events	Chapter 21: Sequences
<b>Assessment</b> 2x 90 minute PPES	<b>Assessment:</b> Chapter A Test	<b>Assessment</b> Chapter A Test
	<p><b>Builds Upon:</b></p> <ul style="list-style-type: none"> <li>• Arrange sets into Venn diagrams</li> <li>• Describe sets using Venn diagrams (intersection, union and complement)</li> <li>• Construct possibility (sample) space diagrams Calculate probabilities from sample space diagrams</li> <li>• Use tree diagrams to show the frequency or probabilities of two events</li> <li>• Use tree diagrams to calculate the probabilities of independent and dependent events</li> </ul>	<p><b>Builds Upon:</b></p> <ul style="list-style-type: none"> <li>• Write sequence using term to term rule</li> <li>• Write sequences using position to term rule (nth rule)</li> <li>• Write the position to term rule (nth rule) for a linear sequence</li> <li>• Recognise special types of sequence (square, cube, triangular, arithmetic, geometric, Fibonacci and quadratic)</li> <li>• Find terms of quadratic sequence using term to term or position to term rule</li> <li>• Write the position to term rule (nth rule) for a quadratic sequence</li> </ul>
	<p><b>Introduces:</b></p> <ul style="list-style-type: none"> <li>• Use Venn diagrams to record outcomes and calculate probabilities of events</li> <li>• Calculate estimated outcomes using probabilities</li> </ul>	<p><b>Introduces:</b></p> <ul style="list-style-type: none"> <li>• Applications to problem solving</li> </ul>

## Spring 1

### Chapter 22: Units and Proportionality

**Assessment:** Chapter A Test

#### **Builds Upon:**

- Calculations using standard and compound units (speed, density and pressure)
- Compare lengths, areas, and volumes of similar shapes
- Solve direct proportion problems
- Interpret the gradient of a straight line graph as a rate of change
- Solve inverse proportion problems

**Introduces:**

- Interpret graphs that illustrate direct and inverse proportion
- Set up, solve and interpret growth and decay problems

## Spring 2

<b>PPES</b>	<b>23: Algebraic Proofs</b>	<b>GCSE EXAM REVISION</b>
<b>Assessment</b> 2x 90minute PPES	<b>Assessment NA</b>	<b>Assessment NA</b>
	<b>Builds Upon</b> <ul style="list-style-type: none"><li>• Algebraic identities</li><li>• Constructing mathematical arguments</li></ul>	<b>Builds Upon:</b> Content informed by QLAs and teacher led
	<b>Introduces</b> <ul style="list-style-type: none"><li>• Counter examples</li><li>• LHS/RHS proofs</li><li>• Odd/Even proofs</li></ul>	<b>Introduces:</b>

## Summer 1

### **GCSE EXAM REVISION**

#### **Assessment:**

**3 x 90 minute formal public exams**

#### **Builds Upon:**

Content informed by QLAs and teacher led

#### **Introduces:**

<b>Summer 2</b>